

# Contents

---

<b>List of Videos</b>	<b>ix</b>
<b>Acknowledgments</b>	<b>xi</b>
<b>About the Authors</b>	<b>xiii</b>
<b>Introduction</b>	<b>1</b>
What Works Best	2
What Works Best When	7
The Path to Assessment-Capable Visible Learners in Mathematics	8
How This Book Works	11
<b>Chapter 1. Teaching With Clarity in Mathematics</b>	<b>17</b>
Components of Effective Mathematics Learning	21
Surface, Deep, and Transfer Learning	21
Moving Learners Through the Phases of Learning	26
<i>Surface Learning in the Middle School Mathematics         Classroom</i>	27
<i>Deep Learning in the Middle School Mathematics         Classroom</i>	29
<i>Transfer Learning in the Middle School Mathematics         Classroom</i>	31
Differentiating Tasks for Complexity and Difficulty	32
Checks for Understanding	36

Profiles of Three Teachers	37
<i>Joanna Halstrom</i>	37
<i>Luciana Fernandez</i>	38
<i>Jasvinder Singh</i>	38
Reflection	40

## Chapter 2. Teaching for the Application of Concepts and Thinking Skills **43**

Ms. Halstrom and Circles and Cylinders	45
<i>What Ms. Halstrom Wants Her Students to Learn</i>	46
<i>Learning Intentions and Success Criteria</i>	47
<i>Guiding and Scaffolding Student Thinking</i>	49
<i>Teaching for Clarity at the Close</i>	53
Ms. Fernandez and Systems of Linear Equations	59
<i>What Ms. Fernandez Wants Her Students to Learn</i>	62
<i>Learning Intentions and Success Criteria</i>	64
<i>Guiding and Scaffolding Student Thinking</i>	65
<i>Teaching for Clarity at the Close</i>	69
Mr. Singh and Integers	78
<i>What Mr. Singh Wants His Students to Learn</i>	79
<i>Learning Intentions and Success Criteria</i>	80
<i>Guiding and Scaffolding Student Thinking</i>	81
<i>Teaching for Clarity at the Close</i>	85
Reflection	91

## Chapter 3. Teaching for Conceptual Understanding **93**

Ms. Halstrom and Circles and Cylinders	94
<i>What Ms. Halstrom Wants Her Students to Learn</i>	95
<i>Learning Intentions and Success Criteria</i>	97
<i>Guiding and Scaffolding Student Thinking</i>	99
<i>Instructional Approaches That Promote Conceptual Understanding</i>	102
<i>Teaching for Clarity at the Close</i>	104

Ms. Fernandez and Systems of Linear Equations	110
<i>What Ms. Fernandez Wants Her Students to Learn</i>	111
<i>Learning Intentions and Success Criteria</i>	112
<i>Instructional Approaches That Promote</i>	
<i>Conceptual Understanding</i>	115
<i>Modeling Strategies and Skills</i>	118
<i>Teaching for Clarity at the Close</i>	122
Mr. Singh and Integers	126
<i>What Mr. Singh Wants His Students to Learn</i>	127
<i>Learning Intentions and Success Criteria</i>	127
<i>Guiding and Scaffolding Student Thinking</i>	128
<i>Instructional Approaches That Promote</i>	
<i>Conceptual Understanding</i>	131
<i>Teaching for Clarity at the Close</i>	133
Reflection	138

## **Chapter 4. Teaching for Procedural Knowledge and Fluency** **139**

Ms. Halstrom and Circles and Cylinders	140
<i>What Ms. Halstrom Wants Her Students to Learn</i>	141
<i>Learning Intentions and Success Criteria</i>	142
<i>Guiding and Scaffolding Student Thinking</i>	143
<i>Instructional Approaches That Promote</i>	
<i>Procedural Fluency</i>	145
<i>Teaching for Clarity at the Close</i>	150
Ms. Fernandez and Systems of Linear Equations	155
<i>What Ms. Fernandez Wants Her Students to Learn</i>	155
<i>Learning Intentions and Success Criteria</i>	156
<i>Modeling Strategies and Skills</i>	158
<i>Guiding and Scaffolding Student Thinking</i>	161
<i>Instructional Approaches That Promote</i>	
<i>Procedural Fluency</i>	163
<i>Teaching for Clarity at the Close</i>	169
Mr. Singh and Integers	173
<i>What Mr. Singh Wants His Students to Learn</i>	173
<i>Learning Intentions and Success Criteria</i>	174

<i>Modeling Strategies and Skills</i>	175
<i>Instructional Approaches That Promote</i>	
<i>Procedural Fluency</i>	177
<i>Teaching for Clarity at the Close</i>	179
Reflection	185
<b>Chapter 5. Knowing Your Impact:</b>	
<b>Evaluating for Mastery</b>	<b>187</b>
What Is Mastery Learning?	188
<i>Using Learning Intentions to Define</i>	
<i>Mastery Learning</i>	189
<i>Establishing the Expected Level of Mastery</i>	190
<i>Collecting Evidence of Progress Toward Mastery</i>	194
Ensuring Tasks Evaluate Mastery	201
Ensuring Tests Evaluate Mastery	203
Feedback for Mastery	205
<i>Task Feedback</i>	207
<i>Process Feedback</i>	209
<i>Self-Regulation Feedback</i>	212
Conclusion	213
Final Reflection	216
<b>Appendices</b>	
A. Effect Sizes	217
B. Teaching for Clarity Planning Guide	222
C. Learning Intentions and Success Criteria Template	227
D. A Selection of International Mathematical	
Practice or Process Standards	228
<b>References</b>	<b>231</b>
<b>Index</b>	<b>233</b>

## List of Videos

### Introduction

Video 1: What Is Visible Learning for Mathematics?

Video 2: Creating Assessment-Capable Visible Learners

### Chapter 1. Teaching With Clarity in Mathematics

Video 3: What Does Teacher Clarity Mean in Middle School Mathematics?

### Chapter 2. Teaching for the Application of Concepts and Thinking Skills

Video 4: Learning Intentions in an Application Lesson

Video 5: Finding the Right Application Task

Video 6: Differentiating in an Application Lesson

Video 7: Facilitating and Evaluating Learning in an Application Lesson

Video 8: Consolidating Deep and Transfer Learning in an Application Lesson

### Chapter 3. Teaching for Conceptual Understanding

Video 9: Aligning a Conceptual Task to the Learning Intention

### Chapter 4. Teaching for Procedural Knowledge and Fluency

Video 10: Differentiating Instruction to Support Surface, Deep, and Transfer Learning

Video 11: Supporting Surface Learning Needs With a Peer Tutor

Video 12: Checking for Understanding as Procedural Knowledge Deepens

Video 13: Supporting Learners' Extension to Transfer

## Chapter 5. Knowing Your Impact: Evaluating for Mastery

Video 14: Evaluating for Mastery

Video 15: Feedback Through Peer-Assisted Reflection

**Note From the Publisher:** The authors have provided video and web content throughout the book that is available to you through QR (quick response) codes. To read a QR code, you must have a smartphone or tablet with a camera. We recommend that you download a QR code reader app that is made specifically for your phone or tablet brand.



Videos may also be accessed at [resources.corwin.com/vmathematics-6-8](https://resources.corwin.com/v/mathematics-6-8)